MODULE DESCRIPTION

|  | Module title |
| :--- | :---: |
| Combinatorics and graph theory | Module code |


| Lecturer(s) | Department where the module is delivered |
| :--- | :--- |
| Coordinator: dr. Gintaras Skersys | Department of Computer Science <br> Faculty of Mathematics and Informatics <br> Other lecturers: |


| Cycle | Type of the module |
| :---: | :---: |
| First | Optional |


| Mode of delivery | Semester or period when the <br> module is delivered | Language of instruction |
| :---: | :---: | :---: |
| Face-to-face | 5,7 semester | Lithuanian |
| Prerequisites: Discrete mathematics | Prequites |  |


| Number of credits <br> allocated | Student's workload | Contact hours | Self-study hours |
| :---: | :---: | :---: | :---: |
| 5 | 130 | 72 | 58 |

## Purpose of the module: programme competences to be developed

Purpose of the module - provide basic combinatorics and graph theory knowledge which will help to study other mathematical and computer science subjects and to read mathematical and computer science literature. It also aims to develop analytical thinking and basic skills needed to independently construct discrete models of the reality and to apply the acquired knowledge in solving practical problems.

## Specific competences:

- Knowledge and skills of underlying conceptual basis (SK4).

| Learning outcomes of the module: <br> students will be able to | Teaching and learning <br> methods | Assessment <br> methods |
| :--- | :--- | :--- |
| To define principal combinatorics and graph theory concepts, to <br> illustrate them by examples. | Lecture <br> Practice classes <br> Individual reading <br> Problem solving <br> Formulate and prove principal combinatorics and graph theory | Test (written) <br> Exam (written) |
| Apply combinatorics and graph theory methods to construct <br> discrete models and to solve practical problems related to them. |  |  |


|  | Contact hours |  |  |  |  |  |  | Self-study work: time and assignments |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Content: breakdown of the topics |  | $\begin{aligned} & \text { 淢 } \\ & \text { E } \end{aligned}$ |  |  | $\begin{aligned} & 3 \\ & \text { 耧 } \\ & 3 \\ & 3 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 3 \\ & 3 \\ & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $n$ 0 0 0 0 0 0 0 0 0 0 | Assignments |
| 1. Arrangements and combinations. Binomial and polynomial coefficients. | 5 |  |  | 4 |  |  | 9 | 8 | Individual reading Problem solving |
| 2. Inclusion-exclusion principle. Examples. | 3 |  |  | 4 |  |  | 7 | 7 |  |
| 3. Stirling numbers. | 3 |  |  | 2 |  |  | 5 | 4 |  |
| 4. Generating functions. Recurrence. | 5 |  |  | 6 |  |  | 11 | 10 |  |
| 5. Basic concepts of graph theory. | 4 |  |  | 4 |  |  | 8 | 7 |  |
| 6 . Forest and trees. Spanning trees. Minimum spanning trees. | 3 |  |  | 4 |  |  | 7 | 6 |  |
| 7. Relations of graph parameters. | 2 |  |  | 2 |  |  | 4 | 4 |  |
| 8. Planar graphs. Euler's theorem. | 2 |  |  | 2 |  |  | 4 | 4 |  |
| 9. Colouring of graphs. | 2 |  |  | 2 |  |  | 4 | 4 |  |
| 10. Number of trees. The Prüfer code of a tree. | 3 |  |  | 2 |  |  | 5 | 4 |  |
| Test |  | 2 |  |  |  |  | 4 |  | 2 hours for tutorial, 2 hours for test. |
| Exam |  | 2 |  |  |  |  | 4 |  | 2 hours for tutorial, 2 hours for exam. |
| Total | 32 | 4 |  | 32 |  |  | 72 | 58 |  |


| Assessment strategy | Weight \% | Deadline | Assessment criteria |
| :---: | :---: | :---: | :---: |
| Test (written) | 50 | During the semester | Test and exam consist of tasks of diverse difficulty (theory questions and exercises). Each task is assessed as follows: $100 \%$ - excellent knowledge and abilities; $75 \%$ - strong knowledge and abilities; <br> $50 \%$ - mediocre knowledge and abilities; <br> $25 \%$ - minimal knowledge and abilities; <br> $0 \%$ - minimal requirements are not satisfied. |
| Exam (written) | 50 | Exam session |  |


| Author | Publis <br> hing <br> year | Title | Number or <br> volume | Publisher or URL |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Required reading | 1996 | Combinatorics lectures (in <br> Lithuanian) | Vilnius: Vilnius university <br> press |  |
| M. Bloznelis | 2006 | Discreet mathematics: basics <br> of combinatorics and graph <br> theory. Lecture notes (in <br> Lithuanian) | $\underline{\text { http://www.mif.vu.lt/katedros/tt }}$ |  |
| E. Manstavičius | sk/bylos/man/files/KOMB- <br> 21.pdf |  |  |  |
| Recommended reading | 2010 | Discrete Mathematics and Its <br> Applications, Sixth Edition | McGraw-Hill Higher Education |  |
| Rosen K.H. | 1996 | Introduction to Graph Theory, <br> Fourth edition | Longman |  |
| Wilson R.J. | 1994 | Combinatorics: Topics, <br> Techniques, Algorithms |  | Cambridge University Press |
| P.J. Cameron |  |  |  |  |

